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GSURE Denoising enables training of higher quality generative priors for accelerated Multi-Coil MRI Reconstruction

Asad Aali¹, Marius Arvinte^{1,2}, Sidharth Kumar¹, Yamin Ishraq Arefeen¹, and Jonathan I. Tamir¹

¹Chandra Family Department of Electrical and Computer Engineering, The University of Texas at Austin, Austin, TX, United States, ²Intel Corporation, Hillsboro, OR, United States

Asad Aali
MS Student
Electrical & Computer Engineering
The University of Texas at Austin



UT Computational Sensing and Imaging Lab

- Joint design of imaging system and software
- Particular focus on application to MRI
- Work with clinicians to translate work to hospital



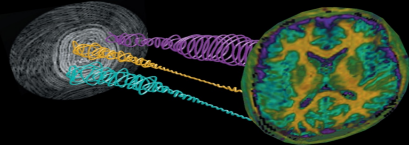
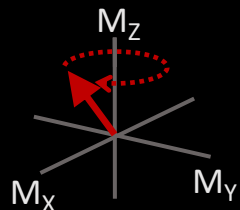
Jon Tamir, PhD
Assistant Professor, ECE, UT Austin
<http://www.jtsense.com/>



<https://github.com/utcsilab>

Computational MRI

Imaging physics



<https://www.nature.com/articles/495184a>

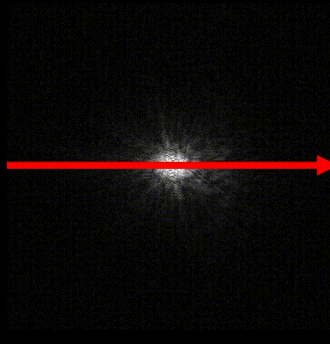


<https://www.aspectimaging.com>

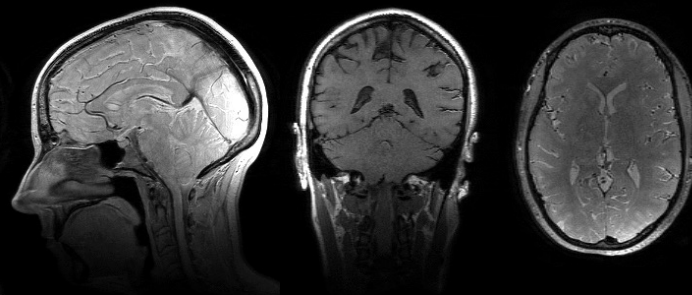


Prior knowledge

Acquisition



Reconstruction



Deep learning inversion for MRI

1. End-to-end supervised training
2. Distribution learning / generative modeling



Generative models are powerful image generators

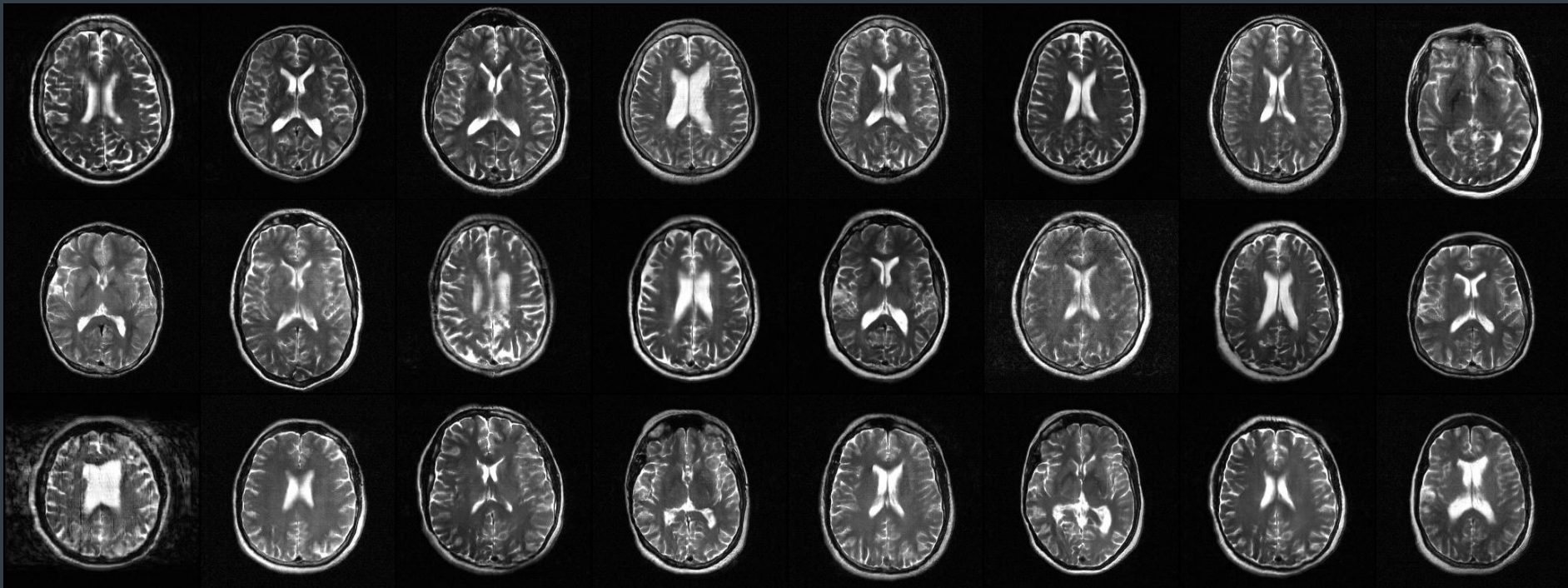


Generative models are powerful image generators



<https://thiscatdoesnotexist.com/>

Generative models are powerful image generators

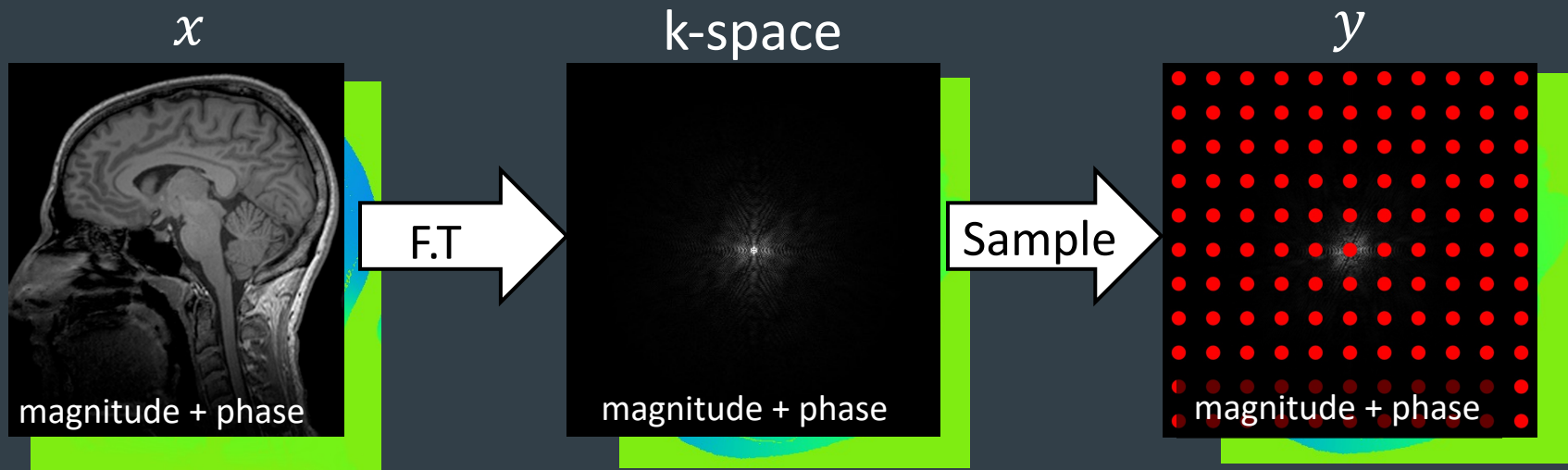


Generative model trained on FastMRI data

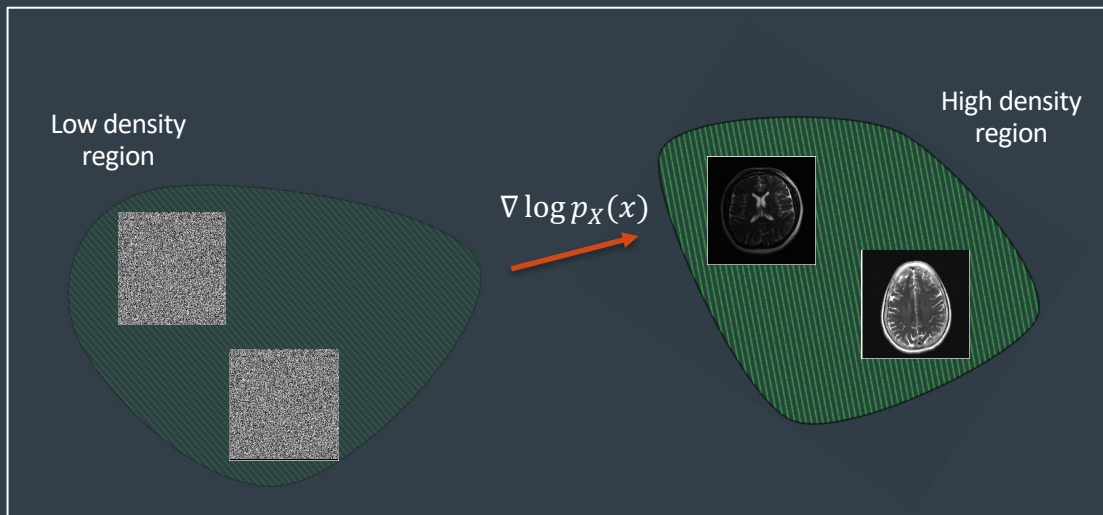
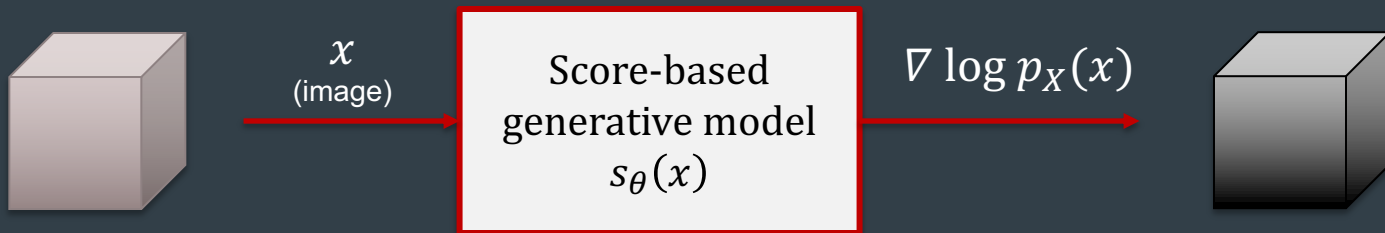
MRI: Problem Formulation

Signal is the Fourier transform of the image

$$y = Ax + \text{noise}$$



Score-based generative models

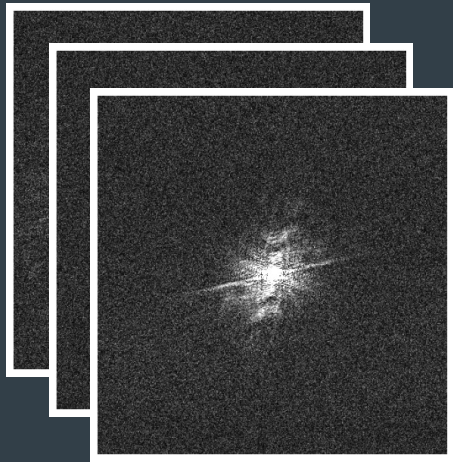


MRI Samples are inherently noisy

Goal is to learn the **clean distribution** using *noisy* data (i.i.d Gaussian, with known power σ_w^2).

$$y = Ax + \textit{noise}$$

y



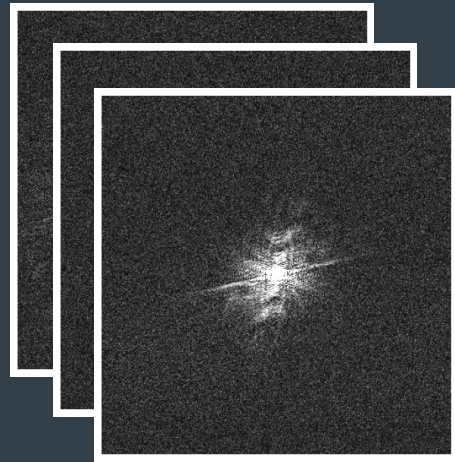
Original K-Space

MRI Samples are inherently noisy

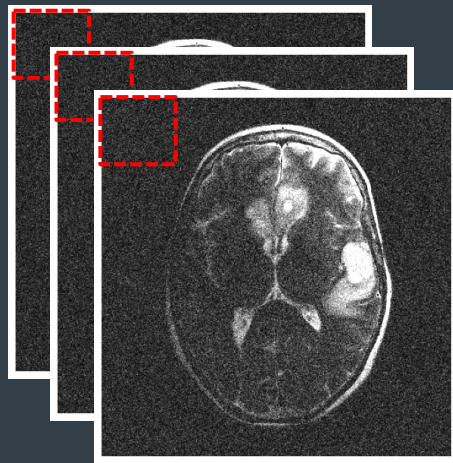
Goal is to learn the **clean distribution** using *noisy* data (i.i.d Gaussian, with known power σ_w^2).

$$y = Ax + \text{noise}$$

 y

 $F^H y$


Original K-Space

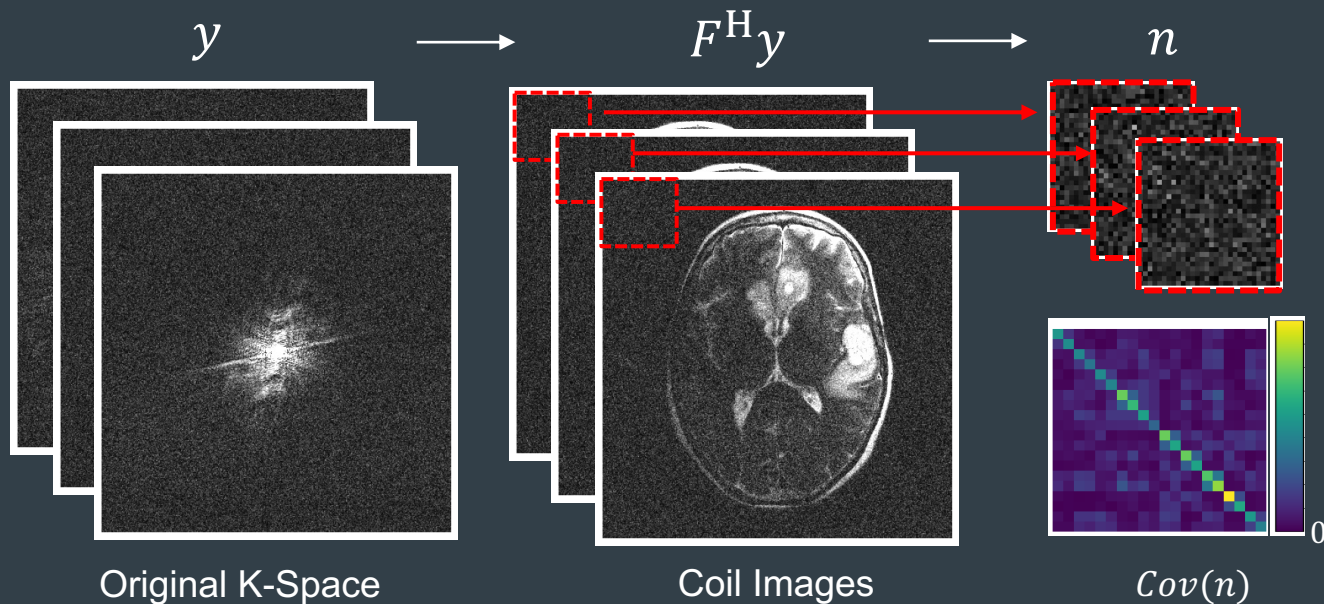


Coil Images

MRI Samples are inherently noisy

Goal is to learn the **clean distribution** using *noisy* data (i.i.d Gaussian, with known power σ_w^2).

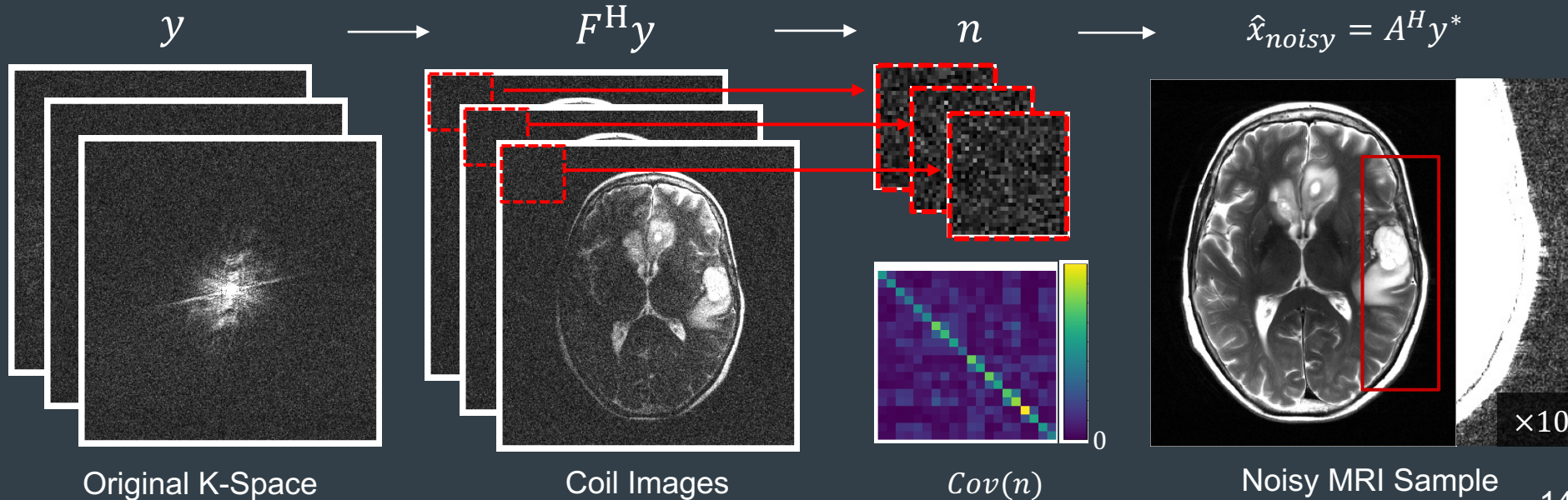
$$y = Ax + \text{noise}$$



MRI Samples are inherently noisy

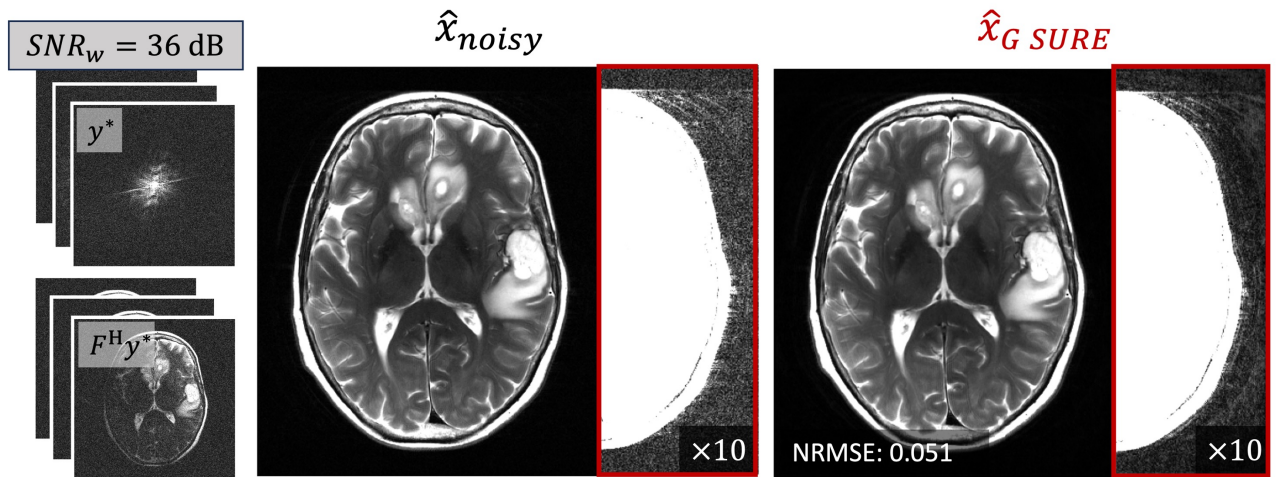
Goal is to learn the **clean distribution** using *noisy* data (i.i.d Gaussian, with known power σ_w^2).

$$y = Ax + \text{noise}$$



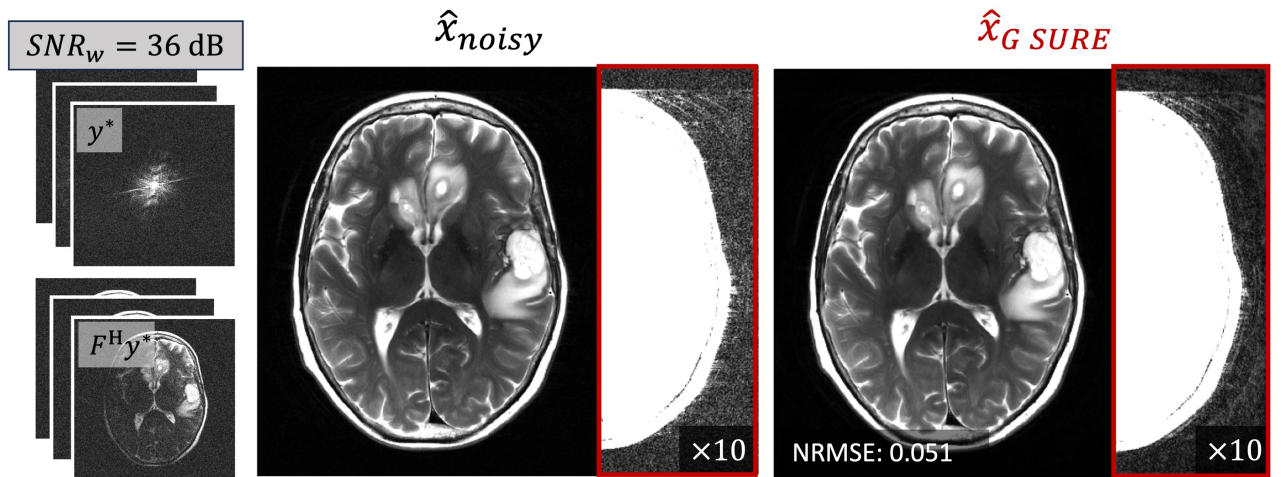
Denoising with GSURE

Original FastMRI



Denoising with GSURE

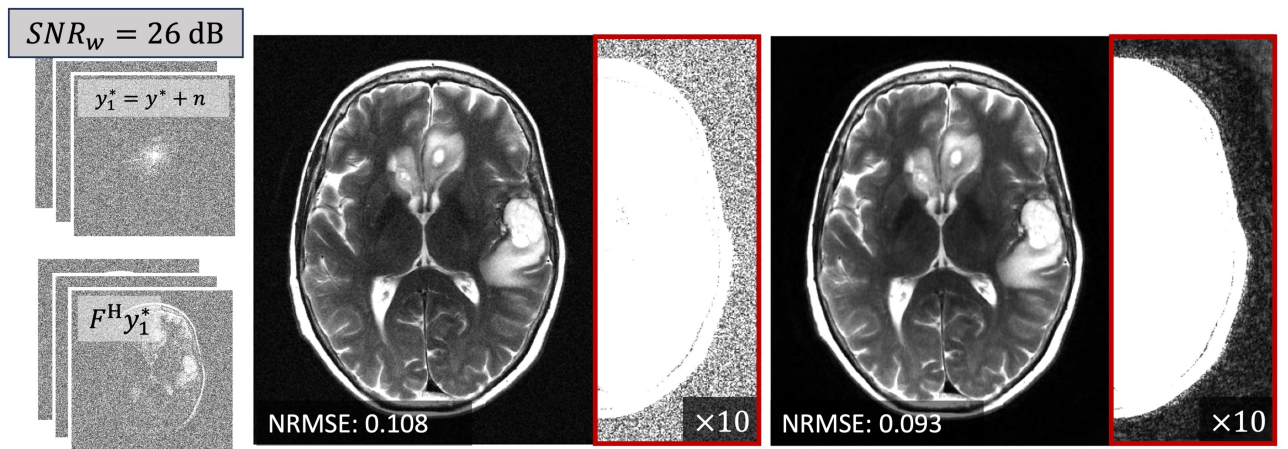
Original FastMRI



Original FastMRI

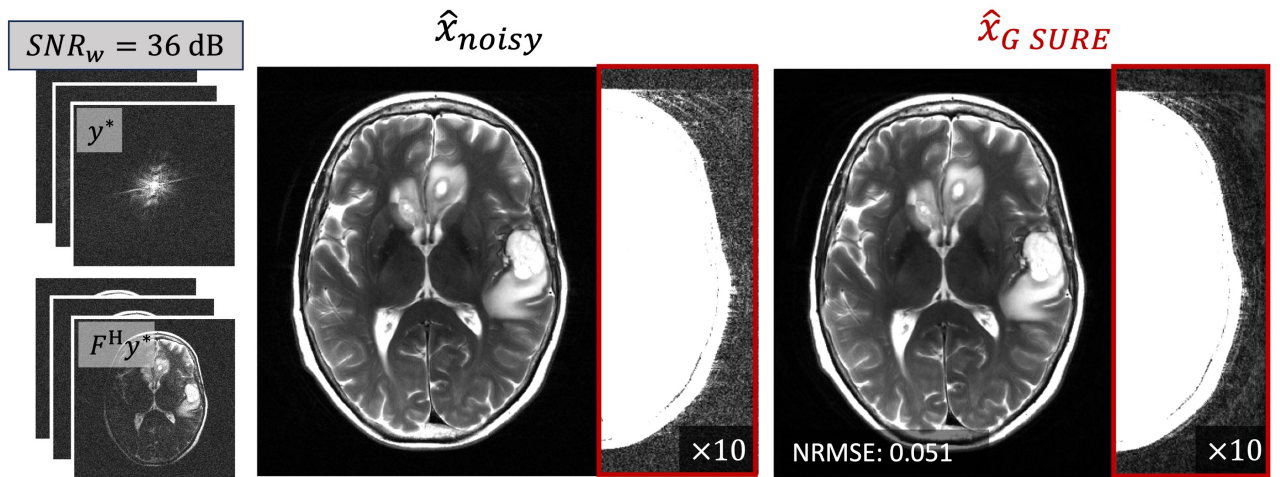
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Additive Gaussian Noise



Denoising with GSURE

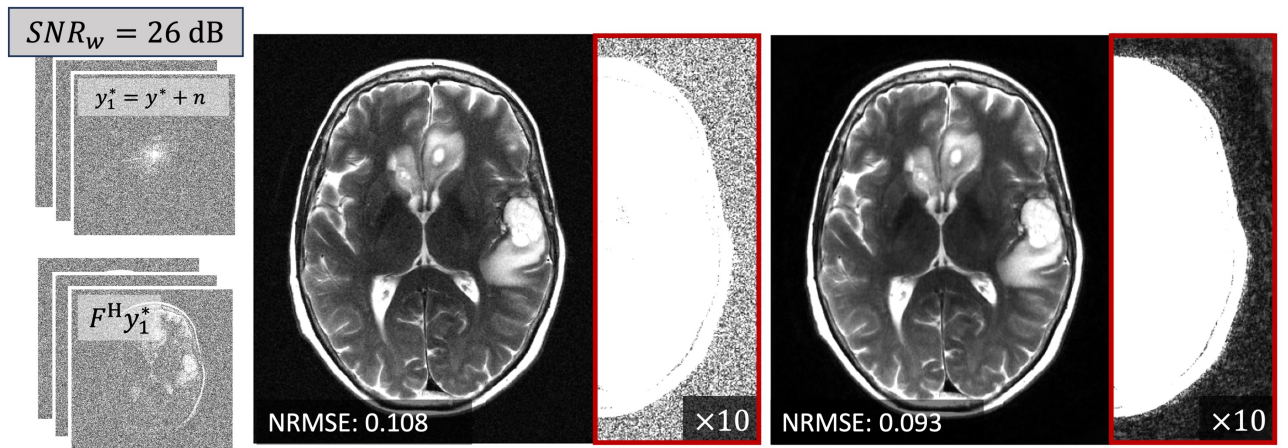
Original FastMRI



Original FastMRI

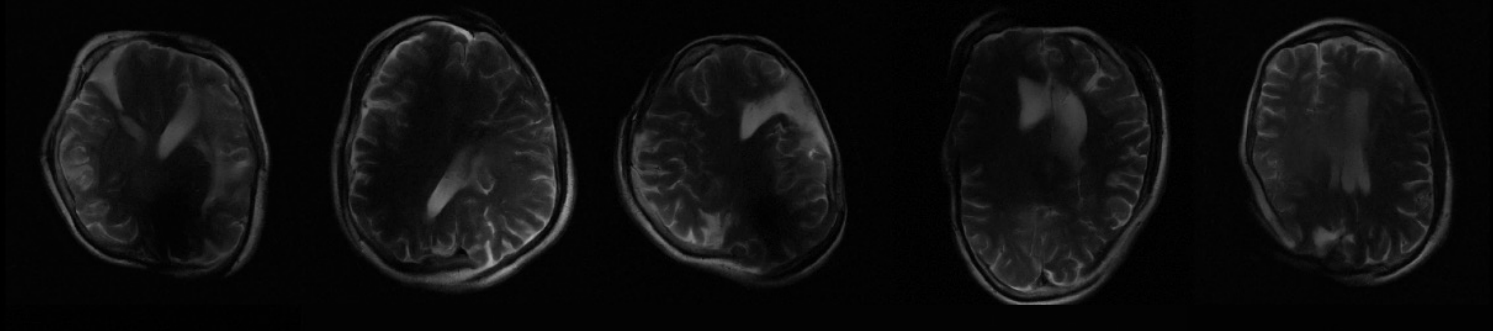
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Additive Gaussian Noise



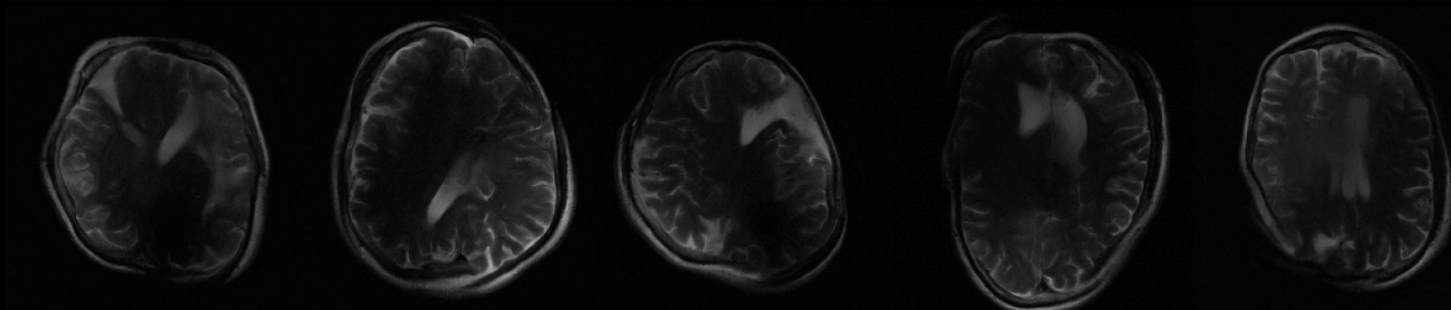
Learning Priors using Generative Models – $p(x)$

Naive Score

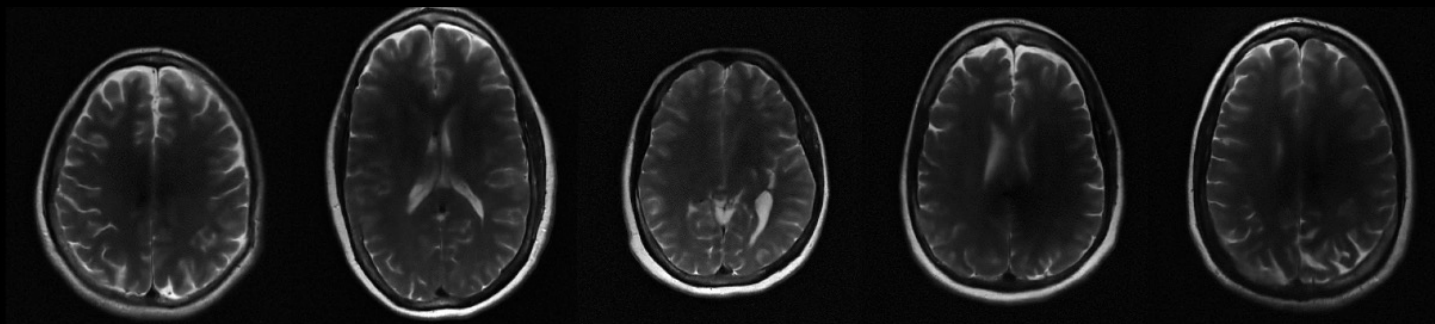


Learning Priors using Generative Models – $p(x)$

Naive Score

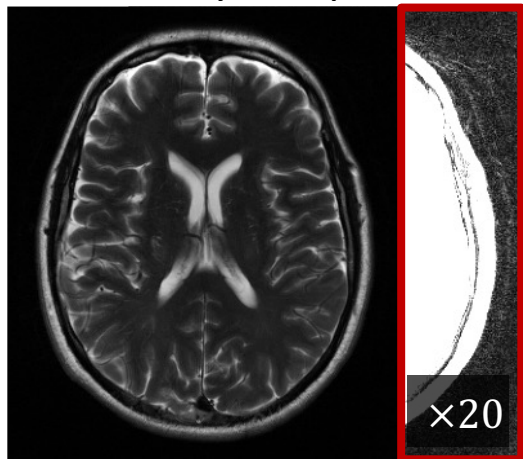


GSURE-Score

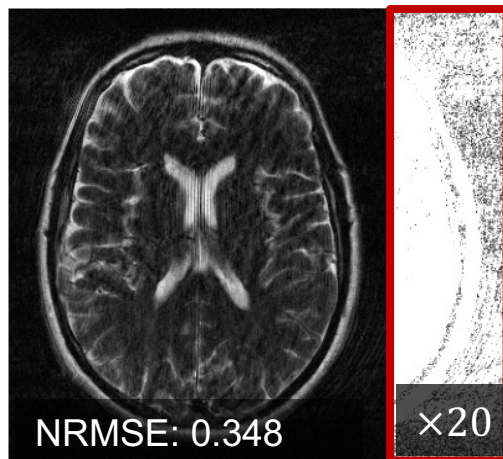


Inverse Problems using Generative Models $x \sim p(x|y)$

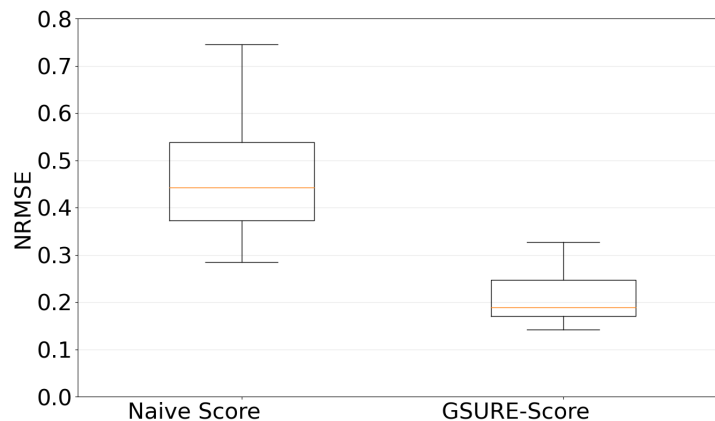
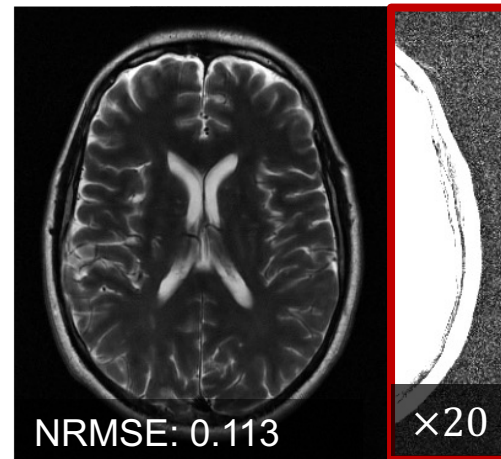
Fully Sampled



Naive Score



GSURE-Score



Conclusions

1. Self-supervised techniques like GSURE can successfully remove noise
2. Denoising as a pre-processing step, severely improves the quality of generative priors
3. Priors trained on denoised FastMRI are better inverse problem solvers than naive training

Thank you!

Asad Aali

asad.aali@utexas.edu

<https://www.linkedin.com/in/asadaali/>

<https://asad-aali.github.io/>

MS ECE Student

The University of Texas at Austin

